

6-2 day 1 Indefinite Integrals and Differential Equations

Learning Objectives:

I can find an indefinite integral

Ex1. Integrate each indefinite integral using integral formulas.

$$1.) \int x^5 dx = \frac{1}{6}x^6 + C$$

$$3.) \int e^{-4x} dx = -\frac{1}{4}e^{-4x} + C$$

$$2.) \int \frac{1}{\sqrt[3]{x}} dx = \int x^{-1/3} dx = \frac{3}{2}x^{2/3} + C$$

$$4.) \int \sin(3x) dx = -\frac{1}{3}\cos(3x) + C$$

$$5.) \int \sec^2\left(\frac{x}{3}\right) dx$$

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What if you cannot evaluate the integral? $\int e^x \sin^3(2x) dx$

We can write the antiderivative as

$$F(x) = \int_0^x e^t \sin^3(2t) dt$$

and look at the graph.

Ex2. Integrate

$$1.) \int (x^2 + 3x + 5) dx = \frac{1}{3}x^3 + \frac{3}{2}x^2 + 5x + C$$

$$2.) \int \left(e^{2x} + \frac{1}{3x}\right) dx = \frac{1}{2}e^{2x} + \frac{1}{3}\ln\left(\frac{3}{2}x\right) + C$$

$$3.) \int (\cos x + \sin x) dx = \sin x - \cos x + C$$

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Ex3. Which integral formulas is correct (if either)?

$$A.) \int \frac{1}{16+x^2} dx = \ln(16+x^2) + C \quad \text{No}$$

$$\frac{1}{16+x^2} \cdot 2x$$

$$B.) \int \frac{1}{16+x^2} dx = \frac{1}{4} \tan^{-1}\left(\frac{x}{4}\right) + C$$

$$\frac{1}{4} \cdot \frac{1}{1+\left(\frac{x}{4}\right)^2} = \frac{1}{16(1+\frac{x^2}{16})} = \frac{1}{16+x^2}$$

Homework

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